

# Centre for Development Economics

*Semiparametric Panel Data Estimation:  
An Application To Immigrants Homelink Effect  
on U.S. Producer Trade Flows*

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## Abstract

In this paper a semiparametric fixed effect estimator is proposed in a partial linear model. The estimator is applied to study the immigrants home-link effect on the U.S. producer trade flows with the home country of the immigrant. The results from this study show that the immigrants support the U.S. producer imports but not the exports. The monte carlo and the asymptotics of the estimator are provided for large  $N$  and fixed  $T$ .

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## 1. INTRODUCTION

Panel data refers to data where we have observations on the same cross-section unit over multiple periods of time. An important aspect of the panel data econometric analysis is that it allows for the cross-section and/or time heterogeneity. Within this framework two types of models are mostly estimated, one is the fixed effect (FE) and the other is the random effect. There is no agreement in the literature as to which one should be used in the empirical work, see Maddala (1987) for a good discussion on this subject. For both types of models there is an extensive econometric literature dealing with the estimation of linear parametric models, although some recent works on the nonlinear and latent variable models have appeared, see Hsiao (1985), Baltagi (1996) and Mátyás and Sevestre (1996). It is, however, well known that the parametric estimators of linear or nonlinear models may become inconsistent if the model is misspecified. With this in view, in this paper we consider only the FE panel models and propose the semiparametric estimators which are robust to the misspecification of the functional forms. The asymptotic properties of the semiparametric estimators are also established.

An important objective of this paper is to explore the application of the pro-

posed semiparametric estimator to study the effect of immigrants "home link" hypothesis on U.S. bilateral trade flows. The idea behind the home link is that when the migrants move to U.S. they maintain ties with their home countries which helps in reducing transaction costs of trade through better trade negotiations, and hence effecting trade positively. In an important recent work, Gould (1994) analyzed the home link hypothesis by considering the well known gravity equation (Anderson (1979) and Bergstrand (1985)) in the empirical trade literature which relates the trade flows between two countries with the economic factors, one of them being transaction cost. Gould specifies the gravity equation to be linear in all factors except transaction cost which is assumed to be a nonlinear decreasing function of the immigrant stock to capture the home link hypothesis.<sup>1</sup> The usefulness of our proposed semiparametric estimators stems from the fact that the nonlinear functional form used by Gould (1994) is misspecified as indicated in Section 3 of this paper. Our findings indicate that the immigrant home link hypothesis holds for producer imports but does not holds for producer exports in the U.S. between 1972-1980.

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<sup>1</sup>Transaction costs for obtaining foreign market information about country  $j$  in the U.S. used by Gould (1994) in his study is given by  $Ae^{-\rho(M/us, j)/(\theta + M_{us, j})}$   $\rho > 0$ ,  $\theta > 0$ ,  $A > 0$  where  $M_{us, j}$  = stock of immigrants from country  $j$  in the United States.

The plan of this paper is as follows. In Section 2 we present the FE model and proposed semiparametric estimators. These semiparametric estimators are then used to analyze the "home link" hypothesis in Section 3. Finally, the Appendix discusses the asymptotic properties of the semiparametric estimators.

## 2. THE MODEL AND ESTIMATORS

Let us consider the parametric FE model as

$$y_{it} = x'_{it}\beta + z'_{it}\gamma + \alpha_i + u_{it}, \quad (i = 1, \dots, n; t = 1, \dots, T) \quad (2.1)$$

where  $y_{it}$  is the dependent variable,  $x_{it}$  and  $z_{it}$  are the  $p \times 1$  and  $q \times 1$  vectors, respectively,  $\beta$ ,  $\gamma$  and  $\alpha_i$  are the unknown parameters, and  $u_{it}$  is the random error with  $E(u_{it} | x_{it}, z_{it}) = 0$ . We consider the usual panel data case of large  $n$  and small  $T$ . Hence all the asymptotics in this paper are for  $n \rightarrow \infty$  for a fixed value of  $T$ . Thus as  $n \rightarrow \infty$ ,  $\sqrt{nT}$  consistency and  $\sqrt{n}$  consistency are equivalent.

From (2.1) we can write

$$Y_{it} = X'_{it}\beta + Z'_{it}\gamma + U_{it} \quad (2.2)$$

where  $R_{it} = r_{it} - \bar{r}_i$ ,  $\bar{r}_i = \sum_t r_{it}/T$ . Then the well known parametric FE estimators of  $\beta$  and  $\gamma$  are obtained by minimizing  $\sum_i \sum_t U_{it}^2$  with respect to  $\beta$  and  $\gamma$  or

$\sum_i \sum_t \dot{u}_{it}^2$  with respect to  $\beta$ ,  $\gamma$  and  $\alpha_i$ . These are the consistent least squares (LS) estimators and they are given by

$$\begin{aligned} b_p &= [\sum_i \sum_t (X_{it} - \bar{X}_{it})(X_{it} - \bar{X}_{it})']^{-1} \sum_i \sum_t (X_{it} - \bar{X}_{it}) Y_{it} \\ &= (S_{X-\bar{X}})^{-1} S_{X-\bar{X}, Y} \\ &= (X' M_Z X)^{-1} X' M_Z Y \end{aligned} \quad (2.3)$$

and

$$c_p = S_Z^{-1} (S_{Z,Y} - S_X b_p) \quad (2.4)$$

where  $p$  represents parametric,  $\bar{X}'_{it} = Z'_{it} (\sum_i \sum_t Z_{it} Z'_{it})^{-1} \sum_i \sum_t Z_{it} X'_{it}$ ,  $S_{A,B} = A' B / nT = \sum_i \sum_t A_{it} B'_{it} / nT$  for any scalar or column vector sequences  $A_{it}$  and  $B_{it}$ ,  $S_A = S_{A,A}$  and  $M_Z = I - Z(Z'Z)^{-1}Z'$ . The estimator  $\hat{\alpha}_i = \bar{y}_i - \bar{x}'_i b_p - \bar{z}'_i c_p$  is not consistent, and this will also be the case with the semiparametric estimators given below.

A new semiparametric estimators of  $\beta$  and  $\gamma$  can be obtained as follows. From (2.2) let us write

$$E(Y_{it} | Z_{it}) = E(X'_{it} | Z_{it})\beta + Z'_{it}\gamma. \quad (2.5)$$

Then subtracting (2.5) from (2.2) we get

$$Y_{it}^* = X_{it}^* \beta + U_{it}, \quad (2.6)$$

which gives the LS estimator of  $\beta$  as

$$\hat{\beta}_{sp} = (\sum_i \sum_t X_{it}^* X_{it}^{*'})^{-1} \sum_i \sum_t X_{it}^* Y_{it}^* = S_{X^*}^{-1} S_{X^*, Y^*} \quad (2.7)$$

where  $R_{it}^* = R_{it} - E(R_{it} | Z_{it})$  and  $sp$  represents semiparametric. We refer to this estimator the semiparametric estimator for the reasons given below.

The estimator  $\hat{\beta}_{sp}$  is not operational since it depends on the unknown conditional expectations  $E(A_{it} | Z_{it})$  where  $A_{it}$  is  $Y_{it}$  or  $X_{it}$ . Following Robinson (1988), these can however be estimated by the nonparametric kernel estimators

$$\hat{A}_{it} = \sum_j \sum_s A_{js} K_{it, js} / \sum_j \sum_s K_{it, js} \quad (2.8)$$

where  $K_{it, js} = K\left(\frac{Z_{it} - Z_{js}}{a}\right)$ ,  $j = 1, \dots, n$ ;  $s = 1, \dots, T$ , is the kernel function and  $a$  is the window width. We use product kernel  $K(Z_{it}) = \prod_{\ell=1}^q k(Z_{it, \ell})$ ,  $k$  is the univariate kernel and  $Z_{it, \ell}$  is the  $\ell$ th component of  $Z_{it}$ . Replacing the unknown conditional expectations in (2.7) by the kernel estimators in (2.8) an operational version of  $\hat{\beta}_{sp}$  becomes

$$\begin{aligned} b_{sp} &= \left( \sum_i \sum_t (X_{it} - \hat{X}_{it})(X_{it} - \hat{X}_{it})' \right)^{-1} \sum_i \sum_t (X_{it} - \hat{X}_{it})(Y_{it} - \hat{Y}_{it}) \quad (2.9) \\ &= S_{X - \hat{X}}^{-1} S_{X - \hat{X}, Y - \hat{Y}} \end{aligned}$$

Since the unknown conditional expectations have been replaced by their nonpara-

metric estimates we refer to  $b_{sp}$  the semiparametric estimator. After we get  $b_{sp}$

$$c_{sp} = S_Z^{-1}(S_{Z,Y} - S_{Z,X} b_{sp}). \quad (2.10)$$

The consistency and asymptotic normality of  $b_{sp}$  and  $c_{sp}$  are discussed in the Appendix.

In a special case where we assume the linear parametric form of the conditional expectation, say  $E(A_{it} | Z_{it}) = Z'_{it} \delta$ , we can obtain the LS predictor as  $\tilde{A}_{it} = Z'_{it} (\sum_i \sum_t Z_{it} Z'_{it})^{-1} \sum_i \sum_t Z_{it} A_{it}$ . Using this in (2.7) will give  $\hat{\beta}_{sp} = b_p$ . It is in this sense  $b_{sp}$  is a generalization of  $b_p$  for the situations where, for example,  $X$  and  $Z$  have a nonlinear relationship of unknown form.

Both the parametric estimators  $b_p$ ,  $c_p$  and the semiparametric estimators  $b_{sp}$ ,  $c_{sp}$  described above are the  $\sqrt{n}$  consistent global estimators in the sense that the model (2.2) is fitted to the entire data set. A local point-wise estimators of  $\beta$  and  $\gamma$  can be obtained by minimizing the kernel weighted sum of squares

$$\sum_i \sum_t [y_{it} - x'_{it} \beta - z'_{it} \gamma - \alpha_i]^2 K\left(\frac{x_{it} - x}{h}, \frac{z_{it} - z}{h}\right) \quad (2.11)$$

with respect to  $\beta$ ,  $\gamma$  and  $\alpha$ ;  $h$  is the window width. The local pointwise estimators so obtained can be denoted by  $b_{sp}(x, z)$  and  $c_{sp}(x, z)$ , and these are obtained by fitting the parametric model (2.1) to the data close to the points  $x, z$ , as

determined by the weights  $K()$ . These estimators are useful for studying the local pointwise behaviors of  $\beta$  and  $\gamma$ , and their expressions are given by

$$\begin{aligned} \begin{bmatrix} b_{sp}(x, z) \\ c_{sp}(x, z) \end{bmatrix} &= \left( \sum_i \sum_t (w_{it} - \hat{w}_i)(w_{it} - \hat{w}_i)' \right)^{-1} \sum_i \sum_t (w_{it} - \hat{w}_i)(y_{it} - \hat{y}_i) \quad (2.12) \\ &= S_{w-\hat{w}}^{-1} S_{w-\hat{w}, y-\hat{y}_1} \end{aligned}$$

where  $w'_{it} = [\sqrt{K_{it}} x'_{it} \sqrt{K_{it}} z'_{it}]$ ,  $K_{it} = K\left(\frac{x_{it}-x}{h}, \frac{z_{it}-z}{h}\right)$ ,  $\hat{A}_i = \sum_t A_{it} K_{it} / \sum_t K_{it}$ .

While the estimators  $b_p$ ,  $c_p$  and  $b_{sp}$ ,  $c_{sp}$  are the  $\sqrt{n}$  consistent global estimators the estimators  $b_{sp}(x, z)$ ,  $c_{sp}(x, z)$  are the  $\sqrt{nh^{p+q+2}}$  consistent local estimators (see Appendix). These estimators also provide a consistent estimator of the semiparametric FE model

$$y_{it} = m(x_{it}, z_{it}) + \alpha_i + u_{it} \quad (2.13)$$

where  $m()$  is the nonparametric regression. This model is semiparametric because of the presence of the parameters  $\alpha_i$ . It is indicated in the Appendix that

$$\hat{m}_{sp}(x_{it}, z_{it}) = x'_{it} b_{sp}(x_{it}, z_{it}) + z'_{it} c_{sp}(x_{it}, z_{it}) \quad (2.14)$$

is a consistent estimator of the unknown function  $m(x_{it}, z_{it})$ , and hence  $b_{sp}$ ,  $c_{sp}$  are the consistent estimators of its derivatives. In this sense  $\hat{m}_{sp}(x_{it}, z_{it})$  is a local linear nonparametric regression estimator which estimates the linear model



(2.1) nonparametrically, see Fan (1992, 1993) and Gozalo and Linton (1994). We note however the well known fact that the parametric estimator  $x'_{it} b_p + z'_{it} c_p$  is a consistent estimator only if  $m(x_{it}, z_{it}) = x'_{it} \beta + z'_{it} \gamma$  is the true model. Same holds for any nonlinear parametric specification estimated by the global parametric method such as nonlinear least squares.

In some situations, especially when the model (2.13) is partially linear in  $x$  but nonlinear of unknown form in  $z$  as in Robinson (1988), we can estimate  $\beta$  globally but  $\gamma$  locally and vice-versa. In these situations we can first obtain the global  $\sqrt{n}$  consistent estimate of  $\beta$  by  $b_{sp}$  in (2.9). After this we can write

$$y_{it}^o = y_{it} - x'_{it} b_{sp} = z'_{it} \gamma + \alpha_i + v_{it} \quad (2.15)$$

where  $v_{it} = u_{it} + x'_{it}(\beta - b_{sp})$ . Then the local estimation of  $\gamma$  can be obtained by minimizing

$$\sum_i \sum_t [y_{it}^o - z'_{it} \gamma - \alpha_i]^2 K\left(\frac{z_{it} - z}{W}\right) \quad (2.16)$$

which gives

$$\begin{aligned} c_{sp}(z) &= \left( \sum_i \sum_t (z_{it} - \hat{z}_i)(z_{it} - \hat{z}_i)' K_{it} \right)^{-1} \sum_i \sum_t (z_{it} - \hat{z}_i)(y_{it}^o - \hat{y}_i^o) K_{it} \quad (2.17) \\ &= S_{\sqrt{K}(z-\hat{z})}^{-1} S_{\sqrt{K}(z-\hat{z})(y^o-\hat{y}^o)} \end{aligned}$$

where  $K_{it} = K\left(\frac{z_{it}-z}{h}\right)$  and  $\hat{A}_i = \sum_t A_{it} K_{it} / \sum_t K_{it}$ . Further  $\hat{\alpha}_i(z) = \hat{y}_i^o - \hat{z}_i' c_{sp}(z)$ .

As in (2.14),  $\hat{m}_{sp}(z_{it}) = z'_{it} c_{sp}(z)$  is a consistent local linear estimator of the

unknown nonparametric regression in the model  $y_{it}^o = m(z_{it}) + \alpha_i + u_{it}$ . But, the parametric estimator  $z'_{it} \hat{\gamma}_p$  will be consistent only if  $m(z_{it}) = z'_{it} \gamma$  is true. For the discussion on the consistency and asymptotic normality of  $b_{sp}(z)$ ,  $c_{sp}(z)$  and  $\hat{m}_{sp}(z)$ , see Appendix.

### 3. EMPIRICAL RESULTS

Here we present an empirical application of our proposed semiparametric estimators. In this application we look into the effect of immigrants "home link" hypothesis on U.S. bilateral producer trade flows. Immigration has been an important economic phenomenon for U.S. with immigrants varying in their origin and magnitude. Crucial force in this home link is that migrants when they move to U.S. maintain ties with their home countries which helps in reducing transaction costs of trade through better trade negotiations, removing communication barriers etc. Migrants also have a preference for home products which should effect U.S. imports positively. There have been studies to show geographical concentration of particular country specific immigrants in U.S. actively participating in entrepreneurial activities, Bonacich etc. (1988). This is an interesting look on the effect of immigration other than the effect on labor market, welfare impacts and might have strong policy implications on supporting migration into U.S. from

one country over another.

The parametric empirical analysis of the "home link" hypothesis was first done by Gould (1994). His analysis is based on the gravity equation (Anderson (1979) and Bergstrand (1985)) extensively used in the empirical trade literature, and it relates the trade flows between two countries with the economic forces, one of them being the transaction cost. Gould's important contribution specifies the transaction cost factor as a nonlinear decreasing function of the immigrant stock to capture the home link hypothesis: decreasing at an increasing rate. Because of this functional form the gravity equation becomes a non-linear model, which he estimates by non-linear least squares using an unbalanced panel of 47 U.S. trading partners.

We construct a balance panel of 47 U.S. trading partners over nine years (1972-1980), so here  $i = 1, \dots, 47$  and  $t = 1, \dots, 9$  giving 423 observations. The country specific effects on heterogeneity is captured by the fixed effect. In our case where  $y_{it}$  = manufactured U.S. producers exports and imports,  $x_{it}$  includes lagged value of producer's exports and imports, U.S. population, home-country population, U.S. GDP, home-country gnp, U.S. GDP deflator, home-country GDP deflator, U.S. export value index, home-country export value index, U.S. import value index, home-country import value index, immigrant stay, immigrant stay

squared, skilled-unskilled ratio of the migrants, and  $z_{it}$  is immigrant stock to U.S. Data on producer manufactured imports and exports was taken from OECD statistics. Immigrant stock, skill level and length of stay of migrants was taken from INS public-use data on yearly immigration. Data on Income prices and population was taken from IMF's International Financial Statistics.

We start the analysis by first estimating the immigrant's effect on U.S. producer exports and imports using Gould's (1994) parametric functional form and plot it together with the kernel estimation, see Figures 1 and 2. The kernel estimator is based on the normal kernel given as  $K\left(\frac{z_{it}-z}{h}\right) = \frac{1}{\sqrt{2\pi}} \exp\left\{-\frac{1}{2}\left(\frac{z_{it}-z}{h}\right)^2\right\}$  and  $h$ , the window-width, is taken as  $cs(nT)^{-1/5}$ ,  $c$  is a constant and  $s$  is the standard derivation for variable  $z$ ; for details on the choice of  $h$  and  $K$  see Härdle (1990) and Pagan and Ullah (1997). Comparing the results with the actual trade flows, we see from Figures 1 and 2 that the functional form assumed in the parametric estimation is incorrect and hence Gould's nonlinear LS estimates may be inconsistent. In fact the parametric estimates,  $b_p$  and  $c_p$ , will also be inconsistent. In view of this we use our proposed  $\sqrt{n}$  consistent semiparametric estimator of  $\beta$ ,  $b_{sp}$ , in (2.9) and the consistent semiparametric local linear estimator of  $\gamma$ ,  $c_{sp}(z)$  in (2.17).

First we look at the semiparametric estimates  $b_{sp}$  given in Table 1. Immi-

grant skilled-unskilled ratio effects exports and imports positively, though it is insignificant. This shows that skilled migrants are bringing better foreign market information. As the number of years the immigrant stays in U. S. increases producer exports and producer imports fall at an increasing rate. It can be argued that the migrants change the demand structure of the home country adversely, decreasing U. S. producer exports and supporting imports. But once the home country information which they carry become obsolete and their tastes change their effect on the trade falls. When the inflation index of a country is going up, the exports from that country might become expensive and are substituted by domestic production in the importing country. Hence when the home-country GDP deflator is going up, U. S. producer imports falls and U. S. GDP deflator effects U. S. producer exports negatively. The U. S. GDP deflator has a positive effect on the U. S. imports that might be due to the elasticity of substitution among imports exceeding the overall elasticity between imports and domestic production in the manufactured production sector in the U. S., whereas the opposite holds in the migrants' home-country. The U. S. export value index reflects the competitiveness for the U. S. exports and has a significant positive effect on producer exports. This maybe due to the supply elasticity of transformation among U. S. exports exceeding the overall elasticity between exports and domestic goods,

which is true for the home-country export unit value index too. The U. S. and the home-country import unit value indexes have positive effect on producer imports and producer exports respectively. This shows that the elasticity of substitution among imports exceeds the overall elasticity between domestic and imported goods both in the U. S. and the home-country. The immigrants home-country GDP effects the producer exports positively and is significant at ten percent level of significance. U. S. GDP effects producer exports negatively and also the home country GDP effects the producer imports negatively showing that the demand elasticity of substitution among imports is less than unity both for the U. S. and its trading partners.

For analyzing the immigrant "home link" hypothesis, which is an important objective here, we obtain elasticity estimates  $c_{sp}(z)$  at different immigrant stock level for both producer's exports and producer's imports. This shows how much U.S. bilateral trade with the  $i - th$  country is brought about by an additional immigrant from that country. Based on this, we also calculate in Table 2 the average dollar value change (averaged over nine years) in U.S. bilateral trade flows:  $\bar{c}_{isp} \times \bar{z}_i$  where,  $\bar{c}_{isp} = \sum_t c_{sp}(z_{it})/T$  and  $\bar{z}_i = \sum_t z_{it}/T$  is the average immigrant stock into the U. S. from the  $i - th$  country. When these values are presented in Figures 3 and 4, we can clearly see that immigrant home link hypothesis supports

immigrant stock effecting trade positively for U.S. producer imports but not for U.S. producer exports. These findings suggest that immigrant stock and U.S. producer imports are complements in general, and producer exports and immigrant from most of the countries are substitutes. In contrast Gould's (1994) nonlinear parametric framework suggests the support for the migrants "homelink hypothesis" for both exports and imports. The difference in our results for exports with those of Gould may be due to misspecification of nonlinear transaction cost function in Gould and the fact that he uses unbalanced panel data. All these results however indicate that "home link" hypothesis alone may not be sufficient to look at the broader effect of immigrant stock on bilateral trade flows. The labor role of migrants and the welfare effects of immigration both in the receiving and the sending country needs to be taken account of. These results also crucially depend on the sample period, during the seventies U. S. was facing huge current account deficits. In any case, the above analysis does open interesting questions as to what should be the U.S. policy on immigration; for example should it support more immigration from one country over the other on the basis of dollar value changes in import or export.

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## A. APPENDIX

Here we present the asymptotic properties of the estimators in Section 2. First we note the well known results that, as  $n \rightarrow \infty$ ,

$$\begin{aligned}\sqrt{nT}(b_p - \beta) &\sim N(0, \sigma^2(P \lim S_{X-\tilde{X}})^{-1}), \\ \sqrt{nT}(c_p - \beta) &\sim N(0, \sigma^2(P \lim S_{Z-\tilde{Z}})^{-1})\end{aligned}\quad (\text{A.1})$$

where  $\tilde{Z}$  is generated by  $\tilde{Z}'_{it} = X'_{it}(\sum_i \sum_t X_{it} X'_{it})^{-1} \sum_i \sum_t X_{it} Z'_{it}$  and  $P \lim$  represents probability limit, see the books by Hsiao (1986) and White (1984).

Next we describe the assumptions that are needed for the consistency and asymptotic normality of  $b_{sp}$ ,  $c_{sp}$ ,  $b_{sp}(x, z)$ ,  $c_{sp}(x, z)$  and  $c_{sp}(z)$  given above. Following Robinson (1988) let  $G_\mu^\lambda$  denote the class of functions such that if  $g \in G_\mu^\lambda$ , then  $g$  is  $\mu$  times differentiable;  $g$  and its derivatives (up to order  $\mu$ ) are all bounded by some function that has  $\lambda - th$  order finite moments. Also,  $K_2$  denotes the class of non-negative kernel functions  $k$  : satisfying  $\int k(v) v^m dv = \delta_{0m}$  for  $m = 0, 1$  ( $\delta_{0m}$  is the Kronecker's delta),  $\int k(v) vv' dv = C_k I$  ( $I > 0$ ), and  $k(u) = O((1 + |u|^{3+\eta})^{-1})$  for some  $\eta > 0$ . Further, we denote  $\int k^2(v) vv' dv = D_k \cdot I$ . We now state the following assumptions:



(A1) (i) for all  $t$ ,  $(y_{it}, x_{it}, z_{it})$  are i.i.d. across  $i$  and  $z_{it}$  admits a density function  $f \in G_{\mu-1}^\infty$ ,  $E(x | z)$  and  $E(z | x) \in G_\mu^4$  for some positive integer  $\mu > 2$  (ii)  $E(u_{it} | x_{it}, z_{it}) = 0$ ,  $E(u_{it}^2 | x_{it}, z_{it}) = \sigma^2(x_{it}, z_{it})$  is continuous in  $x_{it}$  and  $z_{it}$ , and  $u_{it}$ ,  $\eta_{it} = x_{it} - E(x_{it} | z_{it})$ ,  $\xi_{it} = (z_{it} - E(z_{it} | x_{it}))$  have finite  $(4 + \delta)th$  moment for some  $\delta > 0$ .

(A2)  $\bar{k} \in K_\lambda$ ; as  $n \rightarrow \infty$ ,  $a \rightarrow 0$ ,  $na^{4\lambda} \rightarrow 0$  and  $na^{\max(2q-4, q)} \rightarrow \infty$ .

(A3)  $k \in K_2$  and  $k(v) \geq 0$ ; as  $n \rightarrow \infty$ ,  $h \rightarrow 0$ ,  $nh^{q+2} \rightarrow \infty$  and  $nh^{q+4} \rightarrow 0$ .

(A1) requires independent observations across  $i$ , and gives some moment and smoothness conditions. The condition (A2) ensures  $b_{sp}$  and  $c_{sp}$  are  $\sqrt{n}$  consistent. Finally (A3) is used in the consistency and asymptotic normality of  $b_{sp}(x, z)$ ,  $c_{sp}(x, z)$  and  $c_{sp}(z)$ .

Under the assumptions (A1) and (A2), and taking  $\sigma^2(x, z) = \sigma^2$  for simplicity, the asymptotic distributions of the semiparametric estimators  $b_{sp}$  and  $c_{sp}$  follow from Li and Stengos (1996), Li (1996) and Li and Ullah (1996). This is given by

$$\sqrt{nT}(b_{sp} - \beta) \sim N(0, \sigma^2 \Sigma^{-1}) \text{ and } \sqrt{nT}(c_{sp} - \beta) \sim N(0, \sigma^2 \Omega^{-1}) \quad (\text{A.2})$$

where  $\Sigma = E(\eta'_i \eta_i / T)$  and  $\Omega = E(\xi'_i \xi_i / T)$ ;  $\eta'_i = (\eta_{i1}, \dots, \eta_{iT})$ . A consistent estimators for  $\Sigma^{-1}$  and  $\Omega^{-1}$  are  $\widehat{\Sigma}^{-1}$  and  $\widehat{\Omega}^{-1}$ , respectively, where  $\widehat{\Sigma} = \frac{1}{nT} \sum_i \sum_T (X_{it} - \hat{X}_{it})(X_{it} - \hat{X}_{it})' = \frac{1}{nT} \sum_i (X_i - \hat{X}_i)'(X_i - \hat{X}_i)$  and  $\widehat{\Omega} = \frac{1}{nT} \sum_i \sum_T (Z_{it} - \hat{Z}_{it})(Z_{it} - \hat{Z}_{it})'$ .

The semiparametric estimators  $b_{sp}$  and  $c_{sp}$  depend upon the kernel estimators which may have random denominator problem. This can be avoided by weighting (2.5) by the kernel density estimator  $\hat{f}_{it} = \hat{f}(Z_{it}) = \frac{1}{nTah} \sum_j \sum_s K_{it,js}$ . This gives  $\tilde{b}_{sp} = S_{(X-\hat{X})f, (Y-\hat{Y})f}^{-1}$ . In this case  $\widehat{\Sigma}$  will be the same as above with  $X - \hat{X}$  replace by  $(X - \hat{X})\hat{f}$ . Finally under the assumptions (A1) to (A3) and noting that  $(nTh^{q+2})^{1/2}(b_{sp} - \beta) = o_p(1)$ , it follows from Kneisner and Li (1996) that for  $n \rightarrow \infty$

$$(nTh^{q+2})^{-1}(c_{sp(z)} - \gamma(z)) \sim N(0, \Sigma_1) \quad (A.3)$$

where  $\Sigma_1 = \frac{\sigma^2(z)}{f(z)} C_k^{-1} D_k C_k^{-1}$ ,  $C_k$  and  $D_k$  are as defined above. In practice we replace  $\sigma^2(z)$  by its consistent estimator  $\hat{\sigma}^2(z_{it}) = \sum_j \sum_s (y_{js}^o - z_{js} c_{sp}(z_{js}))^2 K_{it,js} / \sum_j \sum_s K_{it,js}$ . Further, denoting  $m(z) = z'\gamma$  and  $\hat{m}_{sp}(z) = z' c_{sp}(z)$ , as  $n \rightarrow \infty$

$$(nTh^q)^{1/2}(\hat{m}_{sp}(z) - m(z)) \sim N(0, \Sigma_2) \quad (A.4)$$

where  $\Sigma_2 = \frac{\sigma^2(z)}{f(z)} \int K^2(v) dv$ , see Gozalo and Linton (1994). Thus the asymptotic variance of  $\hat{m}(z)$  is independent of the parametric model  $z\gamma$  used to get the estimate  $\hat{m}(z)$  and it is the same as the asymptotic variance of Fan's (1992, 1993) nonparametric local linear estimator. In this sense  $c_{sp}(z)$  and  $\hat{m}_{sp}(z)$  are the local linear estimators.

The asymptotic normality of the vector  $[b'_{sp}(x, z), c'_{sp}(x, z)]$  is the same as

the result in (A.3) with  $q + 2$  replaced by  $p + q + 2$  and  $z$  replaced by  $(x, z)$ . As there, these estimators are also the local linear estimators.

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Table 1: Bilateral Manufactured Producer Trade Flows Between the U. S. and the Immigrant Home Countries

Dependent Variable	U. S. Producer Exports		U. S. Producer Imports	
	Parametric Model	SPFE	Parametric Model	SPFE
U.S GDP deflator	0.52 (3.34)	-9.07 (18.22)	-12.42 (9.69)	5.45 (77.62)
Home-country GDP deflator	-0.25 (0.09) <sup>a</sup>	-0.09 (0.06)	0.29 (0.26)	-0.11 (0.35)
U.S GDP	-1.14 (2.13)	-3.29 (11.01)	6.71 (6.71)	5.35 (53.74)
Home-country GDP	0.60 (0.11) <sup>a</sup>	0.17 (0.09) <sup>c</sup>	0.56 (0.34) <sup>b</sup>	-0.16 (0.45) <sup>a</sup>
U.S. population	5.09 (40.04)	88.24 (236.66)	6.05 (123.8)	-67.18 (1097.20)
Home-country population	0.41 (0.18) <sup>a</sup>	0.58 (0.48)	0.58 (0.53) <sup>c</sup>	-5.31 (2.47)
Immigrant stay	-0.06 (0.05)	0.01 (0.25)	-0.16 (0.01)	-0.13 (1.18)
Immigrant stay (squared)	0.002 (0.003)	0.001 (0.02)	0.01 (0.01)	0.003 (0.07)
Immigrant skilled-unskilled ratio	0.01 (0.02)	0.02 (0.02)	0.06 (0.06)	0.02 (0.06)
U.S export unit value index	1.61 (0.46) <sup>a</sup>	1.91 (0.57) <sup>a</sup>		
Home-country import unit value index	-0.101 (0.04)	0.072 (0.09)		
Home-country export unit value index			1.72 (0.77) <sup>a</sup>	0.37 (1.85)
U. S. import unit value index			-0.10 (0.34)	0.004 (0.22)

Newey-West corrected standard errors in the parenthesis. <sup>a</sup>Significant at one percent level. <sup>b</sup>Significant at five percent level. <sup>c</sup>Significant at ten percent level

Table 2: Average Dollar Value change in U. S. Producer Trade Flows from one addition of Immigrant between 1972-1980

COUNTRY		PRODUCER EXPORTS	PRODUCER IMPORTS
1	AUSTRALIA	-84447.2	107852.2
2	AUSTRIA	-257216	332576.7
3	BRAZIL	-72299.9	91995.54
4	CANADA	-1908566	2462421
5	COLOMBIA	-300297	381830.7
6	CYPRUS	-11967.4	15056.1
7	DENMARK	-65996.3	85321.2
8	EL SALVADOR	-115355	146500.3
9	ETHIOPIA	-11396.6	13098.77
10	FINLAND	-93889.6	121071.7
11	FRANCE	-174535	225599.7
12	GREECE	-557482	718292.1
13	HUNGARY	-172638	163015.4
14	ICELAND	-13206.8	17003.16
15	INDIA	-311896	383391.8
16	IRELAND	-577387	742629.5
17	ISRAEL	-126694	159101.8
18	ITALY	-2356589	3045433
19	JAPAN	-446486	575985.8
20	JORDAN	-33074.7	41427
21	KENYA	-3604.1	4044.627
22	MALAYSIA	-9761.78	11766
23	MALTA	-23507.1	30184.8
24	MOROCCO	-2899.56	2797.519
25	NETHERLANDS	-346098	447181.1
26	NEW ZEALAND	-23666.3	30182.7
27	NICARAGUA	-74061.1	93930.9
28	NORWAY	-231098	298533.2
29	PAKISTAN	-35508.4	42682.64
30	PHILIPPINES	-214906	258027.4
31	S. AFRICA	-29243.3	37247.1
32	S. KOREA	-89567.5	109286.9
33	SINGAPORE	-4095.1	4863.85
34	SPAIN	-161804	207276.4
35	SRI LANKA	-7819.8	9685.5
36	SWEDEN	-220653	28500.9
37	SWITZERLAND	-91599.2	118259.2
38	SYRIA	-358830.3	44644.6
39	TANZANIA	-2875.3	2679.2
40	THAILAND	-49734.8	58071.3
41	TRINIDAD	-113210	142938.1
42	TUNISIA	-3285.2	3066.1
43	TURKEY	-115192	147409.5
44	U. K.	0	0
45	W. GERMANY	-1938678	2505652
46	YUGOSLAVIA	-468268	598664.1
47	ZIMBABWE	-2209.5	1997.1



Figure 1

COMPARISON OF U. S. PRODUCER EXPORTS/ PARAMETRIC FUNCITONAL ESTIMATION/  
KERNEL ESTIMATION

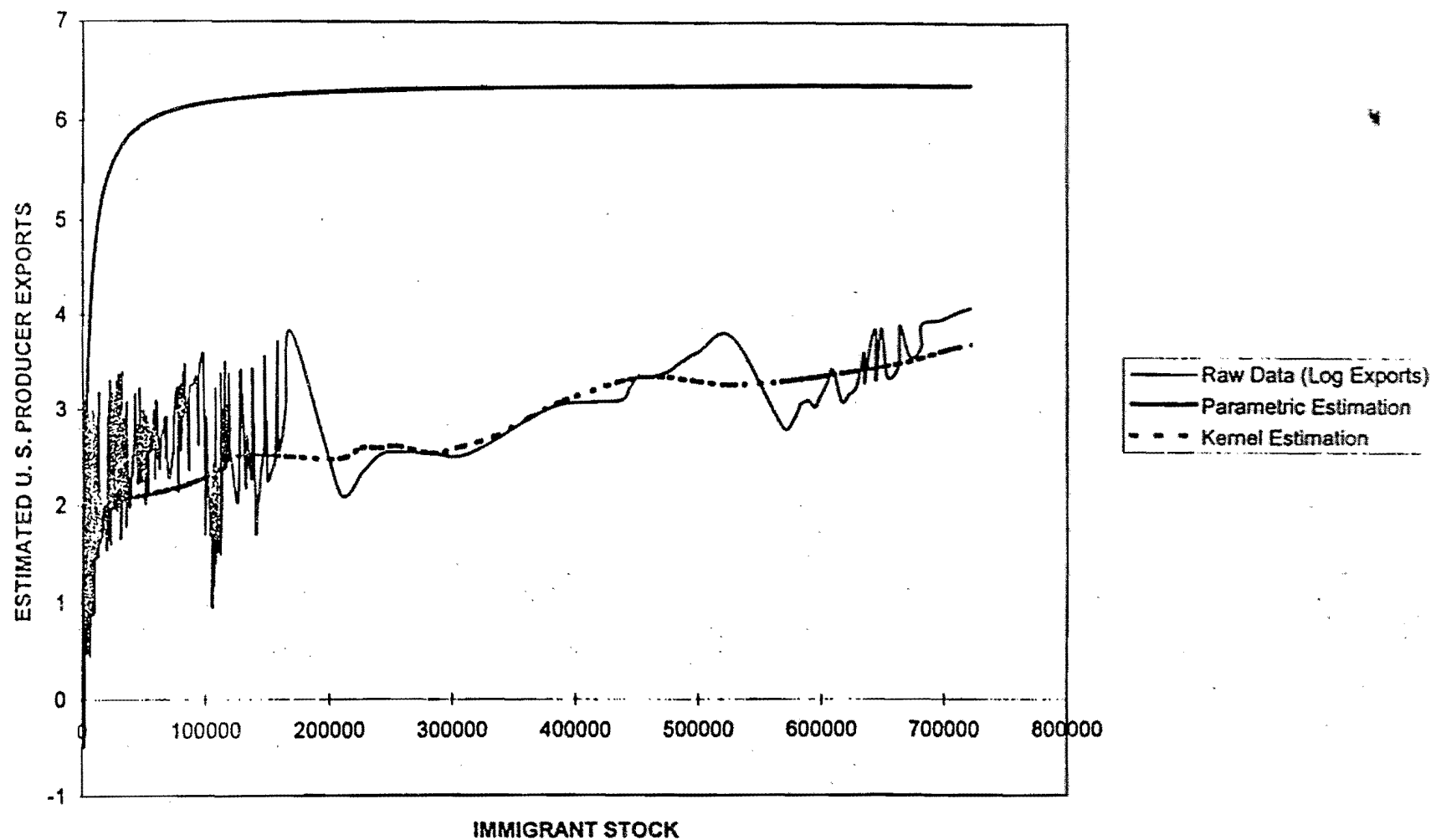


Figure 2

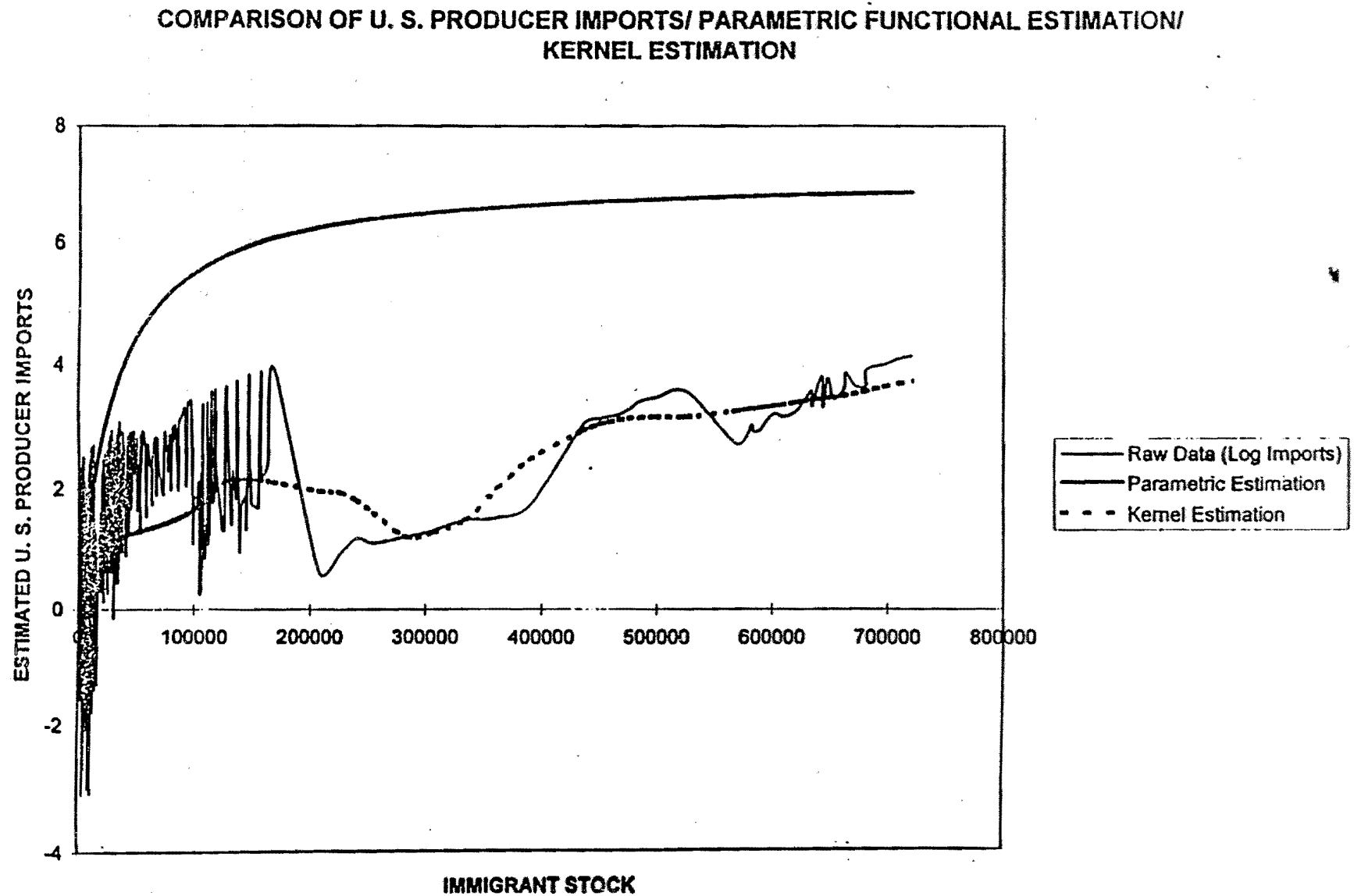


Figure 3: Average Estimated Dollar Value Change in the

# IMMIGRANT STOCK

Figure 3: Average Estimated Dollar Value Change in the U. S. Producer Imports from One Additional Immigrant

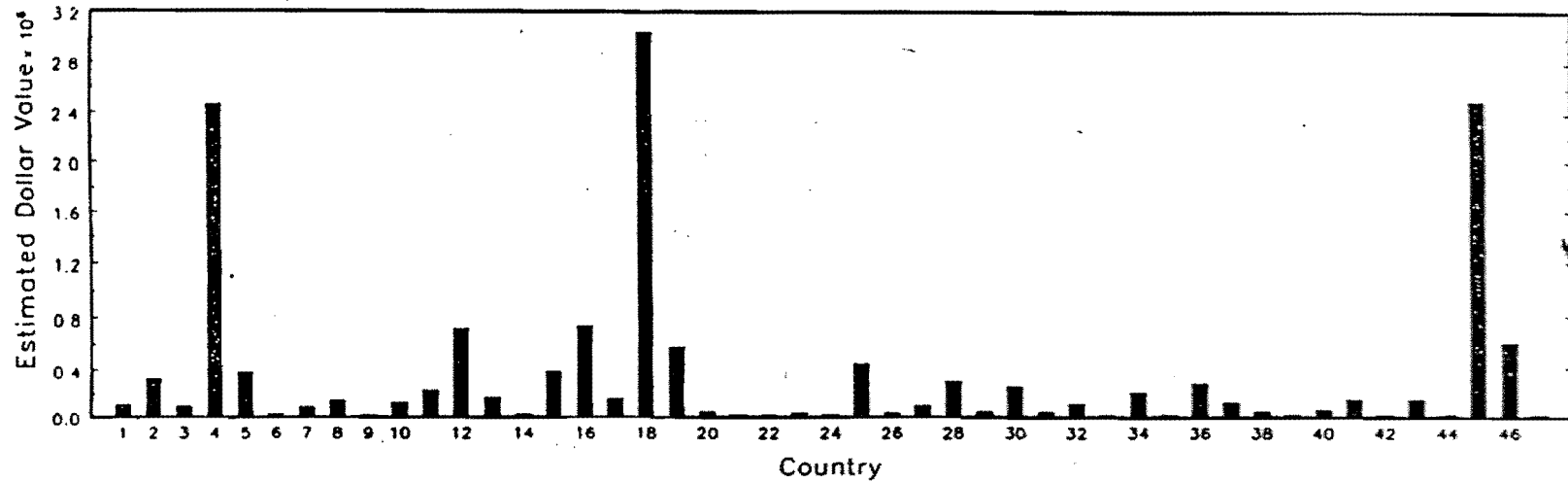
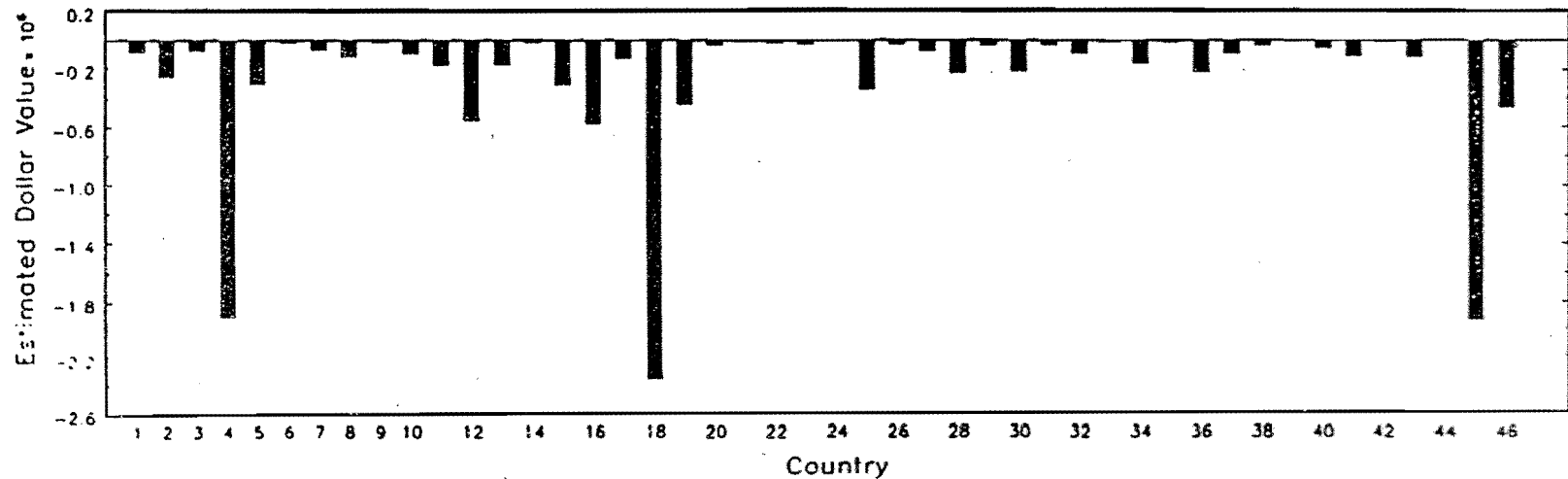


Figure 4: Average Estimated Dollar Value Change in the U. S. Producer Exports from One Additional Immigrant



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